

Gender Equality and Women in STEM: The Curious Case of Arab Women in Israel*

Naomi Friedman-Sokuler[†] and Moshe Justman[‡]

June 28, 2018

Abstract

We document and analyze substantial cultural differences in mathematics gender gaps and how they relate to female participation in advanced STEM matriculation electives. Using administrative longitudinal data on two distinct ethno-linguistic groups, Hebrew and Arabic speakers, within the highly centralized Israeli education system, we find that the gender achievement–gap favoring girls in Arabic schools, the ethnic group characterized by less gender equality, is greater than the gender gap favoring girls in Hebrew schools. Moreover, male-dominated STEM matriculation electives in Hebrew schools are female-dominated in Arabic schools. We show that these patterns are not dependent on socioeconomic or school characteristics but rather a result of ethnic differences in the effect of prior achievement on subject choice by gender. We consider possible cultural sources for these different gendered patterns of education outcomes such as gender-STEM stereotypes and marriage markets.

Keywords: culture, gender gap in mathematics, STEM, Israel, high school, educational choice

JEL Classification Numbers: I21, J15, J16, J24.

*We gratefully acknowledge the financial support of the Rothschild Caesarea Foundation, and the technical support of the Central Bureau of Statistics, and especially Yaffa Shif, Edna Shimoni and David Gordon, in preparing the data and making it available to us. We thank Amal Abu-Tayeh, Ola Hallaq and participants at the annual meetings of the Israeli Economic Association, the American Educational Research Association and the World Educational Research Association; at INET’s Young Scholars Initiative Plenary; at the Melbourne Institute for Applied Economic and Social research; at the InGRID summer school; at the CDED workshop in Groningen; at the XXVI Meeting of the Economics of Education Association; and at the EALE 2017 Conference for their helpful comments and suggestions. None are responsible for any of our findings or conclusions.

[†]Department of Economics, Bar Ilan University, Israel; corresponding author, friedmn6@biu.ac.il

[‡]Department of Economics, Ben Gurion University, Israel and Ruppin Academic Center; justman@bgu.ac.il

1 Introduction

Gender roles in society are culturally conditioned, yet the way in which culture shapes gender roles may be difficult to anticipate. There is a widely observed pattern in advanced industrialized countries, of men dominating mathematically intensive occupations in the workforce, particularly engineering and information technology (Blau and Kahn, 2017). Further evidence shows that these patterns emerge yet earlier, with male students dominating mathematically intensive study fields—such as physics and computer science—in secondary and tertiary education (Turner and Bowen, 1999; Riegle-Crumb *et al.*, 2012; Buser *et al.*, 2014; Friedman-Sokuler and Justman, 2016; Justman and Méndez, 2018; Rapoport and Thibout, 2018). Among industrialized countries, cross-country analysis indicates that the male advantage in mathematical achievement in secondary education decreases with general measures of gender equality in society (Guiso *et al.*, 2008; Nollenberger *et al.*, 2016). However, Fryer and Levitt (2010) this pattern disappears when the analysis includes predominantly Muslim countries characterized by low levels of gender equality.

The case of Arab women in Israel, which we consider here, presents an opportunity to investigate the sources of this puzzle within a unique institutional setting. Arab society in Israel, while in transition from a traditional-patriarchal to a modern society, is still characterized by distinctively lower gender equality compared to the Hebrew-speaking majority by all measures, as are other Middle Eastern countries (Abu-Baker and Azaiza, 2010; Yashiv and Kasir, 2011). Yet, as we show in this paper, students in Arabic-language schools, the ethnic group characterized by *less* gender equality, exhibit gender patterns *favoring* women, with respect to STEM achievement and choice. In this study, we are able to attribute these patterns to differences in cultural norms rather than institutional factors due to the fact that both ethnic groups study within a similar institutional setting and the use of a rich and comprehensive data set, allowing us to control for socio-economic and early achievement differences between groups.

Using a longitudinal administrative data set, we follow two half-cohorts of Israeli youth attending Arabic-language and Hebrew-language schools, from the eighth grade, when they sit for standardized tests in mathematics, reading, science and English, to the twelfth-grade, when they

are tested in matriculation electives chosen during the three years of high school. We find that while students in Hebrew-language schools follow similar patterns to those found in advanced industrialized countries, students in Arabic-language schools exhibit a larger female advantage in mathematics, even after controlling for differences in socio-economic background. Moreover, Arab women have a greater relative propensity to choose traditionally male-dominated STEM matriculation electives—physics, computer science and advanced mathematics—where Hebrew speaking women are very much underrepresented. This reversal is anticipated to some extent by the substantial female advantage in mathematics achievement in Arabic-language middle schools, but it is qualitatively robust to the inclusion of prior test scores and background characteristics. Finally, while in Hebrew-language the gender gaps favoring men in physics, computer science and advanced mathematics electives schools increases in early mathematical achievement, in Arabic-language schools gender gaps favoring men are non-existent and even reversed among top achieving students.

Our empirical approach follows the epidemiological analysis used by Fernández and Fogli (2009) and Nollenberger *et al.* (2016), to identify the effect of culture on outcomes by comparing immigrants from different cultural backgrounds acting within the same institutional setting. While the two ethnic groups study in different schools—segregated by language—they share the same institutional setting. The schools in our data set—both Hebrew- and Arabic-language schools—are coeducational,¹ and they operate under the supervision of a single, centralized ministry of education, with similar spending per student, following the same curriculum in STEM subjects, and taking the same matriculation tests (except for translation). Their teachers belong to the same union, study at the same universities and most attend the same teacher training programs.² These institutional constraints suggest that the remaining differences between Hebrew- and Arabic-language schools stem from different cultural norms.

These findings contribute to the existing literature in several ways. First, the experience of Arab

¹We exclude from this analysis Hebrew religious and ultra-orthodox schools, the overwhelming majority of which are segregated by gender.

²This holds for high school teachers, which are the relevant teachers for this study.

women in Israel belies the notion of a general female disadvantage in mathematics, or of a general female aversion to STEM subjects such as physics and computer science (Ceci *et al.*, 2014), highlighting instead the role of culture in shaping the gendered patterns of education achievement and choice. Second, most of the quantitative analysis on the emergence of gender gaps in educational achievement and choice applies to western cultural groups in developed countries, where cultural variation is limited to the normative framework of western culture. The unique context of Israeli society offers the opportunity to compare western cultural norms to traditional-patriarchal norms, while holding the institutional setting fixed. Furthermore, the longitudinal nature of our data set allows us to compare gendered choice patterns while controlling for early achievement within large population cohorts. Our findings align with and elaborate the pattern that Fryer and Levitt (2010) revealed: an inverse relation between traditional measures of gender equality, such as female labor force participation, and gender gaps in mathematical achievement and educational choices.

Interestingly, this pattern does not follow through to subsequent stages: Arab women are currently as under-represented in engineering programs in tertiary education, and in engineering and IT occupations in the workforce, as much as Hebrew-speaking women. This indicates that these differences are not motivated by a greater availability of jobs in STEM occupations for Arab women, though this may change as the supply of qualified Arab women grows, and there is greater demand for STEM capabilities. Quantitative and qualitative research in behavioral science suggests a number of specific channels through which culture affects the educational subject choices of Arab women, including their value in the marriage market, and differences between Arab and Western culture in the gender stereotyping of mathematically-intensive occupations. Therefore, our analysis of achievement and choice among Arab students contributes to the public discussion of gender gaps in the Arab world and among immigrant from these regions, highlighting the potential for increasing the participation of women in mathematically intensive fields in these societies.

The remainder of the paper proceeds as follows: Section 2 describes the Israeli context. Section 3 describes the student population and the construction of the study sample. Section 4 presents the main educational outcomes, and the unconditional ethnic and gender gaps. Section 5 outlines

our estimation strategy, and analyses the evolution of gender gaps in achievement from eighth to twelfth grade and the choice of STEM matriculation electives. Section 6 analyzes gender and ethnic heterogeneity in the relationship between prior achievement and choice. Section 7 discusses potential mechanisms driving the ethnic differences in gender gaps. Section 8 concludes.

2 The Israeli context

The population of Israel comprises two major ethnic groups, with limited contact between them: Jews who account for 74.9% of the population, and Arabs who account for 20.7%.³ The Arab minority is predominantly Muslim (83%), with the rest Christian and Druze, in equal proportions (Central Bureau for Statistics, 2015). The Arab minority resides overwhelmingly in distinct geographical localities, and the small percentage who live in 'mixed cities' usually live in segregated neighborhoods. The two ethnic groups are linguistically distinct, Jews and non-Arab Christians speak Hebrew whereas Muslims, Arab Christians and Druze are native Arabic speakers. Overall, Hebrew speakers are characterized by substantially higher average income and education levels than the Arab population (Gharrah, 2015).

Hebrew speaking society in Israel is generally characterized as Western-democratic, where Arab society is more traditional and patriarchal-hierarchical (Oyserman, 1993; Dwairy, 1997; Fogiel-Bijaoui, 2002; Cinamon, 2009). Jewish men and women, the large majority of Hebrew-speakers, share the role of wage earners and caretakers of the home and family to a greater extent than in Arab society, which defines women as dependent, as belonging to particular men, and as nurturers and caretakers of both their husbands and children (Abu-Baker, 1998; Kalekin-Fishman, 2004; Cinamon, 2009). In line with this, Arab sons are raised to be the future breadwinners, where daughters are generally expected to continue the traditional roles of their mothers. Arab girls' freedom of movement is limited to the home or the family enclave where they are under direct supervision (Dwairy, 2004).

³The remaining 4.4% are non-Arab Christians, individuals with unclassified religion and others. These groups generally live and study as part of the Jewish majority.

These cultural differences are reflected in a variety of indicators regarding gender roles.⁴ Age at first marriage is highest among Jews, 25.9, and lowest among Muslims, 21.7 years. In 2013, 7.5% of Jewish women were married by the age of 19, compared to 12.3% of Muslim women (Central Bureau for Statistics, 2015; Gharrah, 2015). The average age of mothers at first birth follows a similar pattern (Central Bureau for Statistics, 2015). When comparing labor-force participation in the prime working-age group, aged 25-54, Jewish men and women are nearly identical, 87.9% and 87.7% respectively, whereas in the Arab population the male rate is more than twice the female rate, 81.8% versus 38.4% (Central Bureau for Statistics, 2015). With regard to political representation, in 2015, 27% of Jewish members of parliament were women, compared to 12.5% among Arab members of parliament; and in municipal government women constitute 14.7% of council members in Jewish municipalities, while in Arab municipalities women account for less than 1% of council members.

Both language sectors are served by a common, centralized education system administered by a national Ministry of Education, with regard to budget, curriculum, structure, teacher supervision and labor relations.⁵ Virtually all Arabic-language schools are co-educational (Shir, 2014), as are all non-religious Hebrew-language schools, on which we focus in this paper.⁶ In the past, Arabic-language schools received substantially less financial and material resources than Hebrew-language schools, but this gap has narrowed in recent years (Lavy, 1998; Blass *et al.*, 2010; Justman, 2014), stemming both from the political marginalization of Arabs in Israel and from the difficulty Arabic-language schools have in obtaining funds from supplemental sources such as local councils, community institutions, non-profit organizations, and philanthropic foundations (Benavot and Resh, 2003).

In primary and secondary school, the two ethnic groups attend separate schools that teach in

⁴Cf. United Nations Economic Commission for Europe (2015).

⁵In 2011, the OECD estimated that 50% of all decisions in lower secondary schools in Israel were made at the ministry level, compared to an average of 36% among OECD countries (OECD, 2016)

⁶There are three types of Hebrew-language schools: state (69%), state-religious (17%) and ultra-orthodox (14%) (Central Bureau for Statistics, 2003). The latter two are characterized by single sex classrooms or schools and are therefore not included in our analysis. In general, Jewish parents choose the type of school their children attend according to their religious orientation.

different languages—Hebrew and Arabic—but follow the same curriculum in mathematics, science and English.⁷ There are curricular differences between Hebrew and Arabic schools in history and literature, but the most substantial difference is in the language curriculum.⁸ In the final years of secondary school, students in both Hebrew- and Arabic-language schools take the national matriculation exams. Full matriculation, a prerequisite for university admissions, requires a passing score in seven basic-level mandatory subjects, and in at least one advanced-level elective. Levels of difficulty are expressed as numbers of units studied in a subject, generally between one and five; an advanced-level elective is an elective taken at the level of five units.⁹ Israeli high schools have some autonomy in choosing the matriculation elective subjects they offer, in accordance with demand and the availability of qualified teachers.

3 The data; background variables

The sources of data for our analysis are two administrative data sets managed by the Israel Ministry of Education: the universe of students enrolled in the eighth grade in two consecutive school years, 2001/2 and 2002/3 (we refer to them in what follows as 2002 and 2003); and matriculation records of students enrolled in the twelfth grade in 2005/6 and 2006/7. These two sets were linked for our study by Israel’s Central Bureau of Statistics using national Identity Numbers. The fundamental ethno-linguistic distinction in this analysis is based on school affiliation in eighth grade—attendance at a Hebrew-language or Arabic-language school.¹⁰ Among Hebrew-language schools, we consider only state non-religious schools, almost all of which are co-educational, ex-

⁷There are seven bilingual schools in Israel, in which Jews and Arabs study together in both languages. Six of the seven schools are elementary schools, up to sixth grade. The seventh continues through high school and belongs administratively to the Hebrew-language sector.

⁸In Arabic schools, the first language is Arabic; in third grade students begin learning Hebrew as a mandatory second language; and in fourth grade they begin studying English as a mandatory third language. In Hebrew-language schools, English is taught as a mandatory second language starting in the fourth grade and Arabic is optional as a third language from fifth grade.

⁹There are over 50 electives available to students, in the natural and exact sciences, social sciences, additional foreign languages (mainly Arabic for Hebrew-speakers and French), geography, art and others.

¹⁰The data we use also records students’ religion as recorded in the population registry. Among Jewish students, 0.06% attended eighth grade in an Arabic language school; among Muslim, Arab-Christian and Druze students, 1.01% attended a Hebrew-language school.

cluding from our analysis gender-segregated Jewish ultra-orthodox and state religious schools, so as to avoid the confounding influence of single-sex education.¹¹ Arabic language schools are almost all coeducational (Shir, 2014).¹²

Our full population comprises 166,269 students, two cohorts of students enrolled in eighth grade in Arabic- and Hebrew-language state schools during the school years 2002 and 2003, of whom 51.7% were male, and 26.7% attended Arabic language schools (Table 1). In the eighth grade, we observe for these students: parents' years of education, school attended by the student and its characteristics, municipality of residence, and country of birth. In 2002 and 2003 the ministry of education implemented the Growth and Efficiency Measures in Schools (GEMS) standardized testing scheme. All publicly funded schools in Israel with an eighth grade, except Jewish ultra-orthodox schools and special education schools, were split into two balanced samples of equal size, with half the schools participating in GEMS in 2002 and the other half in 2003. For students who took at least one of the four GEMS tests we also observe the family income quintile.¹³ We also observe for all students in both cohorts who attended twelfth grade four years after attending eighth grade (in 2006 and 2007, respectively): the school they attend in the twelfth grade, eligibility for a matriculation certificate, level of difficulty of each mandatory subject, science electives chosen and their level of difficulty, and scores in the different matriculation tests.¹⁴

Our measures of eighth-grade achievement are individual scores in the four GEMS tests: Reading (native language skills in Hebrew/Arabic), Mathematics, English, and Science and Technology. Half of the schools were tested in 2002 and the other half in 2003. We refer to the students enrolled in these schools as the GEMS sample. It includes 85,012 students of whom 51.5% are male and 25.5% attend Arabic-language schools. The drop in the share of Arab students, compared to the

¹¹We also do not include special education schools. Differences in gender streaming patterns between Jewish state and state-religious schools are analyzed in Feniger (2010) and Friedman-Sokuler and Justman (2016).

¹²In our study sample, 4% of students in Arabic-language schools and 2% of students in Hebrew-language schools attend single-sex schools. We include them in our sample to avoid selection; omitting these students has no effect on our results.

¹³Family income is the gross income of both parents as reported to the Israel Tax Authority. Income quintiles were defined over the population of students participating in GEMS in 2002 and 2003.

¹⁴We observe matriculation outcomes only for students who enrolled in the twelfth grade four years after attending eighth grade. In Israel, repeating or skipping a grade in secondary school is rare. Students migrating to Israel between the eighth and twelfth grades are excluded from our study.

full population, is due to the fact that some of the Arabic Church schools, attended by about 4% of the Arab student population, did not participate in the first years of the GEMS assessment but appear in our full population.¹⁵ Table 1 shows that for students attending Hebrew-language schools, differences in parental education between the full population and the GEMS sample are negligible, while in Arabic schools, the average levels of parental education are slightly lower in the GEMS sample. This decline is because the Arabic Church schools that did not participate in these waves of GEMS enroll children from families with above-average education and income. For students in our full population who attended twelfth grade four years after eighth grade we observe twelfth grade outcomes, but not eighth grade scores. In Appendix A1, we analyze the effect of attrition on female-to-male achievement and choice ratios in twelfth-grade, and find that it has little effect.

Finally, to obtain the study sample, we also drop students enrolled in GEMS schools for whom we have no data on parental education or fewer than two of the four GEMS scores.¹⁶ Over a third of students in Hebrew schools in the GEMS sample, and nearly a quarter of students in Arabic schools, have only two or three GEMS scores (see Table A2 in the Appendix), and for these we impute the missing scores from the scores we have and from student background variables, separately for Hebrew and Arabic schools.¹⁷ Where we have both parents' years of education, we use the larger value as our explanatory variable; where we have education for only one parent we use that value. This leaves us with a study sample of 68,050 students of whom 50.3% are male and 24.2% attended Arabic-language schools. Comparing the GEMS sample to the study sample we see that there is attrition at the lower end of the socio-economic distribution for both Arabs and Jews and more so for boys in each language sector. Consequently GEMS scores are

¹⁵The Arabic Church schools are considered elite schools in Arab society in Israel. They are fee-paying schools, owned by various churches and partially funded by the Ministry of Education. These schools are attended by both Christians and Muslims. The average share of Christian students in Arabic-language schools that did not participate in either wave of GEMS is 39%, compared to 12% in all Arabic-language schools.

¹⁶Table A2 in the Appendix shows attrition patterns from the GEMS sample to the study sample. We drop 15% of the GEMS sample for whom we have less than two GEMS scores, and an additional 9% of the sample for missing family background.

¹⁷We impute missing GEMS scores by regressing each GEMS score on the other scores and on all available background characteristics for students with all scores, and use the regression to predict missing scores. Adding school fixed effects made very little difference to the imputed values. Qualitatively, our results are robust to limiting the sample to students with all four GEMS score.

Table 1: Family characteristics

	Hebrew schools						Arabic schools					
	Female			Male			Female			Male		
	Full sample	GEMS sample	Study sample	Full sample	GEMS sample	Study sample	Full sample	GEMS sample	Study sample	Full sample	GEMS sample	Study sample
Father's years of education	12.89 (2.97)	12.9 (2.95)	12.96 (2.90)	12.88 (2.97)	12.89 (2.96)	13.02 (2.92)	9.85 (3.20)	9.67 (3.11)	9.73 (3.08)	9.83 (3.24)	9.64 (3.12)	9.8 (3.12)
Mother's years of education	13.04 (2.81)	13.06 (2.78)	13.13 (2.72)	13.04 (2.80)	13.06 (2.78)	13.2 (2.74)	9.29 (2.98)	9.1 (2.88)	9.11 (2.85)	9.22 (3.00)	9.03 (2.92)	9.13 (2.91)
Parents' maximal years of education	13.58 (3.00)	13.6 (2.97)	13.67 (2.91)	13.59 (3.00)	13.61 (2.99)	13.76 (2.95)	10.39 (3.10)	10.21 (3.01)	10.26 (2.98)	10.34 (3.15)	10.16 (3.03)	10.31 (3.02)
Income quintile												
Lowest	—	12.3%	11.5%	—	12.0%	10.8%	—	42.6%	40.4%	—	41.8%	39.0%
2nd	—	17.9%	17.4%	—	17.6%	17.1%	—	29.7%	30.6%	—	29.7%	30.4%
3rd	—	20.8%	20.9%	—	21.4%	21.4%	—	17.2%	17.9%	—	17.7%	18.7%
4th	—	23.5%	24.1%	—	23.7%	24.4%	—	7.8%	8.2%	—	8.2%	8.9%
Highest	—	25.4%	26.2%	—	25.4%	26.3%	—	2.8%	2.9%	—	2.7%	3.0%
Christian-Arab*	—	—	—	—	—	—	9.0%	4.0%	5.0%	8.0%	5.0%	5.0%
Immigrant**	22.7%	22.4%	20.3%	22.3%	21.9%	19.7%	0.5%	0.3%	0.3%	0.4%	0.4%	0.4%
N	58,759	30,690	25,529	63,103	32,669	26,061	21,592	10,529	8,270	22,815	11,124	8,190
2002 share	50.0%	48.4%	48.2%	50.2%	51.8%	48.8%	46.8%	48.6%	47.7%	47.5%	47.5%	49.0%
Gender share	48.2%	48.4%	49.5%	51.8%	51.6%	50.5%	48.6%	48.6%	50.2%	51.4%	51.4%	49.8%

*Christian-Arab refers to student's religion as recorded in the population registry. **Immigrants are students born outside of Israel.

slightly lower in the GEMS sample than in the study sample, with differences ranging from 0.02 standard deviations for girls in Hebrew-language schools to 0.06 standard deviations for boys in Arabic-language schools (Appendix Table A2).

In each of the three groups in Table 1—the full population, the GEMS sample and the study sample—the two ethnic groups are socio-economically distinct. Parents of students in Hebrew schools have, on average, three more years of schooling than parents of students in Arabic schools. Moreover, while in Hebrew-language schools mothers are slightly more educated than fathers, the opposite is true in Arabic-language schools. In terms of family income, the differences are even starker. Only 10% of students in Arabic schools are in the top two income quintiles, compared to half of the students in Hebrew schools. When moving from the GEMS sample to the study sample, we see that among both Hebrew- and Arabic-language students, boys’ socio-economic status (SES) improves more than girls’ SES. This is due to the fact that boys are more likely to have fewer than two GEMS scores (see Table A2 in the appendix), an indicator for absenteeism that is highly correlated with SES. Consequently in both ethnic groups, the difference between boys’ and girls’ SES is slightly larger in the study sample.

4 Outcome measures

The two language sectors also differ substantially in the educational outcomes we analyze here: eighth-grade test scores and end-of-high-school attainment and choice of matriculation electives. Table 2 presents eighth-grade achievement levels by ethnicity and gender. In all eighth-grade subjects, the ethnic gaps in favour of Hebrew schools are sizeable, ranging from 0.46 of a standard deviation in science to 0.79 in English.¹⁸ Table A2 in the Appendix shows that the gender-ethnic gaps in the study sample are nearly identical to those of the full GEMS sample. In both ethnic groups, girls outperform boys, and to a larger extent in the language arts—native language and English. However, the gaps are larger in Arabic-language schools, especially in mathematics and

¹⁸The larger gap in English is a result of English being a third language in Arabic schools (Hebrew is the second), where it is the second language in Hebrew schools.

science, where Arab girls outperform boys by 0.26 and 0.34 of a standard deviation respectively, compared to 0.07 and 0.04 of a standard deviation in Hebrew-language schools. These findings accord with the previous cross-sectional findings of Birenbaum and Nasser (2006), Birenbaum *et al.* (2007) and Rapp (2015), indicating an advantage in mathematics for Hebrew-language schools and for girls, with a larger advantage for girls in Arabic-language schools.

Table 2: Eighth grade scores in GEMS (standard deviations in parentheses)

	Hebrew schools			Arabic schools		
	Female	Male	Gender gap*	Female	Male	Gender gap*
Mathematics GEMS	53.75 (23.33)	52.11 (24.79)	0.07	41.61 (22.22)	35.81 (22.51)	0.24
N	23,017	22,751		7,493	7,803	
Science GEMS	65.00 (17.82)	64.28 (20.15)	0.04	59.22 (19.57)	51.70 (22.32)	0.38
N	22,634	22,218		7,515	7,790	
Reading GEMS	67.91 (18.01)	59.52 (20.48)	0.39	56.00 (21.83)	42.54 (22.91)	0.62
N	23,622	23,621		7,492	7,694	
English GEMS	81.92 (18.75)	77.16 (22.2)	0.21	66.12 (21.23)	57.11 (24.08)	0.40
N	23,104	22,934		7,481	7,691	

$$*\text{Gender gap} = \frac{(\text{female average} - \text{male average})}{\text{pooled standard deviation}}$$

At the end of high school, Arab students have significantly weaker outcomes, on average, than Hebrew-language students; and Arab boys have significantly weaker outcomes than all other groups. The top panel of Table 3 shows that Arab boys drop out at a substantially higher rate than any other group. In both language sectors, girls are more likely to matriculate than boys in their group but the gaps are much wider in Arabic schools. These gaps change markedly with respect to the share of students choosing matriculation electives in science. As Table 3 shows, Arab students choose science electives at a higher rate than students in Hebrew-language schools.

Moreover, where girls in Hebrew-language schools are less likely to choose a science or mathematics elective than boys, this is not the case in Arabic-language schools. Almost two thirds of girls and over half the boys in Hebrew-language schools matriculate without taking any science elective, where in Arabic language schools the shares of girls and boys who matriculate without taking a science elective are similar, and both are under 30%. Moreover, there are substantial differences between language sectors in the choice of specific science electives. The share of students choosing advanced mathematics and computer science is substantially higher in Hebrew-language schools where in Arabic-language schools a larger share choose biology and chemistry.

Table 3: Twelfth grade attainment and choice

	Hebrew schools			Arabic schools		
	Female	Male	Gender gap*	Female	Male	Gender gap*
Reached the twelfth grade	0.94	0.89	0.05	0.92	0.76	0.16
Matriculation certificate	0.67	0.55	0.12	0.50	0.28	0.22
Science elective**	0.29	0.35	-0.07	0.60	0.40	0.19
Matriculation with no STEM as a share of those matriculating	0.44	0.29	0.15	0.14	0.08	0.05
	0.66	0.53	0.13	0.28	0.29	-0.01
Physics	0.05	0.13	-0.08	0.08	0.07	0.01
Computer science	0.04	0.11	-0.07	0.03	0.20	0.00
Biology	0.14	0.08	0.06	0.33	0.18	0.15
Chemistry	0.08	0.06	0.02	0.17	0.08	0.09
Physics or computer science	0.07	0.18	-0.11	0.09	0.08	0.01
Biology or chemistry	0.19	0.13	0.06	0.41	0.22	0.19
Advanced mathematics (5 units)	0.14	0.16	-0.02	0.12	0.08	0.04

$N = 68,050$ All shares are with respect to the eighth-grade population in the study sample.

* Gender gap = female share – male share, percentage points

** Science electives = share of students taking any of these four science electives exams even if final matriculation is incomplete.

Gendered choice patterns vary markedly between the two ethnic groups. In the selection of

physics and computer science, girls in Hebrew-language schools are under-represented at a rate of 2.6 to one, while girls in Arabic schools are slightly more likely to choose these subjects than Arab boys. In Hebrew-language schools, 16% of boys and 14% of girls choose the highest level of mathematics, 5 units, while among Arabs, girls are the majority at this level, 12% to 8%. In biology and chemistry, girls are overrepresented in both sectors, and more so in Arabic schools. For the purpose of the current analysis, we pool advanced physics with advanced computer science, and advanced biology with advanced chemistry. The two subjects in each pair exhibit similar gender patterns and combining categories simplifies the presentation of our results and increases statistical power.¹⁹

5 Estimation

To isolate the cultural component of the gender gaps in achievement and streaming patterns, we apply a variation of the epidemiological approach used by Antecol (2000) and Fernández and Fogli (2006, 2009), and expanded in Fernández (2011), to identify cultural effects on individual choices and outcomes by comparing descendants of immigrants from different countries living in the same country. Here we apply this approach to cultural variation between two native ethnic groups differing in religion and language but studying in schools run by the same (centralized) ministry of education.

5.1 Main specification

Given the socio-economic differences between the two groups, our main specification, equation (1), applies a difference-in-difference regressions to estimate the difference, δ , between gender

¹⁹These are also the two most common combinations of electives. Most results hold qualitatively also for each elective separately. Note that selection within categories may also reflect restricted choice, as fewer schools offer chemistry or computer science than offer biology or physics. We adopted a similar approach in Friedman-Sokuler and Justman (2016).

gaps in the two ethnic groups.

$$y_{is} = \beta_0 + \beta_F Female_i + \beta_A Arab_i + \delta Female * Arab_i + \mathbf{X}_i \boldsymbol{\theta} + \mathbf{A}_i \boldsymbol{\gamma} + \mathbf{S}_s \boldsymbol{\lambda} + \eta_t + u_{is} \quad (1)$$

Here y_{is} is the educational outcome of student i in school s , $Female$ is an indicator for whether a student is female and $Arab$ for whether the student attends an Arabic school in eighth grade, \mathbf{X}_i is a vector of socio-economic characteristics and η_t is a year fixed effect. For twelfth grade outcomes we add a vector of the student's prior achievement, \mathbf{A}_i , and in some specifications we also add school-school level characteristics, \mathbf{S}_s . The error term, u_{is} , is clustered at the school level. The coefficient of interest, δ , estimates the difference in the female advantage between Arabic and Hebrew language schools, controlling for socio-economic characteristics and, in twelfth grade, prior achievement.

Equation 1 implicitly assumes that the effect of SES and prior achievement is homogeneous across gender. However, Friedman-Sokuler and Justman (2016) found that in Hebrew-language schools the size of the gender gap increases in parental education, and more steeply in the male-dominated subjects, advanced mathematics and physics or computer science, indicating that boys benefit more from a strong family background.²⁰ The literature suggests two potential explanations for this phenomenon. The first relates to gender differences in non-cognitive skills, resulting in males having higher rates of developmental problems, disruptive behavior, attention disorders, reading disabilities, and other related phenomena which may be amplified when combined with dimensions of social disadvantage correlated with fewer years of parental education (Goldin *et al.*, 2006; DiPrete and Jennings, 2012). In addition, as occupational segregation and the gender pay-gap are more pronounced in jobs that do not require post-secondary education, girls may face stronger incentives to invest in secondary education (Dwyer *et al.*, 2013). To allow for heterogeneity in the effect of socio-economic characteristics by gender, we use equation (2) to estimate the

²⁰We also tested for differences by language sector, but this did not change the mean ethnic differences in gender gaps. Results are available upon request. In section 6, our analysis of heterogeneity considers each of the four gender-language groups separately.

ethnic gap separately for male and female students, where g represents female or male;

$$y_{is}^g = \beta_0^g + \beta_A^g Arab + \mathbf{X}_i \boldsymbol{\theta}^g + \mathbf{A}_i \boldsymbol{\gamma}^g + \mathbf{S}_s \boldsymbol{\lambda}^g + \eta_t^g + u_{is}^g \quad g = F, M \quad (2)$$

Here $\beta_A^F - \beta_A^M$ is the counterpart of δ in equation (1): the difference in the "Arab" effect between female and male students, controlling for socio-economic characteristics and prior achievement, and allowing for differences in marginal effects by gender.

For ease of interpretation, all equations are estimated using OLS when eighth-grade scores are the dependent variables, and a linear probability model when twelfth-grade binary outcomes are the dependent variable.²¹ We also estimated the same choice model using a multinomial logistic regression model, with "no matriculation" as the baseline outcome. This did not alter the sign or significance of our results, but we prefer the single outcome framework, as matriculation electives are not mutually exclusive.

5.2 Ethnic differences in gender gaps in eighth-grade achievement

The top panel of Table 4 presents coefficient estimates from equation (1) for each of the four standardized GEMS scores: β_F , the gender gap in Hebrew-language schools; β_A , the ethnic achievement gap; and δ , the ethnic difference in gender gaps.²² The gender gap in Arabic language schools is substantially higher than in Hebrew-language schools, by 0.16 of a standard deviation in mathematics to a third of a standard deviation in science, and the differences are statistically significant. Conditioning estimates on socio-economic characteristics, in the even numbered columns, substantially reduces the disadvantage of Arab students in the different subjects (β_A), but the ethnic differences in gender gaps remain unaltered. Adding up the three coefficients in the even-numbered columns, we find that conditional on SES, achievement of Arab girls is similar to that of boys in Hebrew-language schools in all subjects except reading, where Arab girls perform substantially

²¹Coefficients' signs and significance as well as predicted probabilities do not differ substantially when estimated using a logistic regression framework. Results are available upon request

²²The full outputs for the four GEMS domains of Equation 1 can be found in Table A3.

better.

Table 4: Ethnic differences in gender gaps in eighth-grade GEMS scores, conditioned on socio-economic indicators

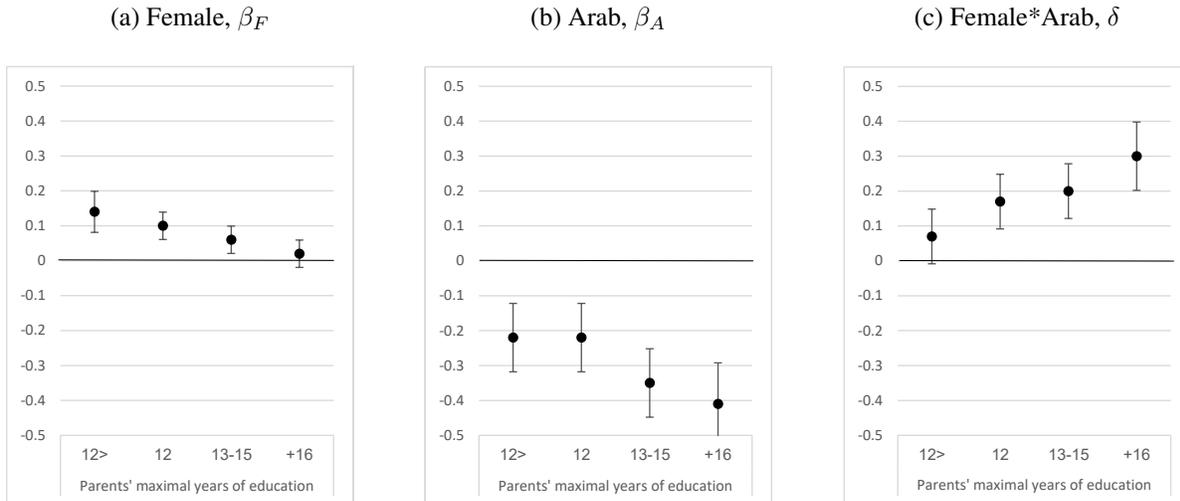
	Mathematics		Science		Reading		English	
	(1)	(2)	(1)	(2)	(1)	(2)	(1)	(2)
	Difference in Difference estimates							
Female, β_F	0.07*** (0.01)	0.08*** (0.01)	0.04** (0.01)	0.05*** (0.01)	0.38*** (0.01)	0.39*** (0.01)	0.20*** (0.01)	0.21*** (0.01)
Arab, β_A	-0.66*** (0.04)	-0.27*** (0.04)	-0.62*** (0.04)	-0.27*** (0.04)	-0.77*** (0.04)	-0.43*** (0.04)	-0.86*** (0.05)	-0.46*** (0.05)
FemaleXArab, δ	0.17*** (0.03)	0.16*** (0.02)	0.34*** (0.03)	0.33*** (0.02)	0.23*** (0.02)	0.23*** (0.02)	0.18*** (0.02)	0.18*** (0.02)
	Ethnic gaps by gender (β_A^g)							
Females, β_A^F	-0.49*** (0.05)	-0.13** (0.05)	-0.28*** (0.04)	0.04 (0.04)	-0.54*** (0.04)	-0.23*** (0.04)	-0.68*** (0.04)	-0.32*** (0.04)
Males, β_A^M	-0.66*** (0.04)	-0.25*** (0.04)	-0.62*** (0.04)	-0.25*** (0.04)	-0.77*** (0.04)	-0.41*** (0.04)	-0.86*** (0.05)	-0.42*** (0.05)
$\beta_A^F - \beta_A^M$	0.17	0.12	0.34	0.29	0.23	0.18	0.18	0.10
Controls								
SES		✓		✓		✓		✓
N		61,064		60,157		62,429		61,210
Share female		0.500		0.499		0.502		0.500

Notes: Dependent variables vary by column and are standardized GEMS scores. Coefficients are obtained from a linear regression model with school-level clustered standard errors and a dummy for cohort. Family SES variables include family income quintiles, parents' maximal years of schooling and immigrant status. Standard errors in parentheses.

* $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$

The bottom panel of Table 4 estimates equation (2) separately for male and female students. While in columns (1) the ethnic difference in gender gaps, $\beta_A^F - \beta_A^M$, is identical to that estimated in the top panel, $\beta_A^F - \beta_A^M$, allowing slopes to vary by gender, in columns (2), slightly reduces this estimate by 0.04 of a standard deviation in mathematics and science, and up to 0.08 of a standard deviation in English—the score increase with SES is steeper among male students than among female students. This finding indicates that between 12% to 44% of the ethnic difference in gender gaps favoring girls in Arab schools can be attributed to Arab boys being adversely affected by the lower socio-economic status of the Arab population more than girls.

Figure 1: Gender and ethnic gaps in GEMS mathematics scores, by parents' education



Notes: Dots represent point estimates of coefficients from Equation 1, by subsample with 95% confidence intervals. All estimates are conditioned on family income quintiles, parents' maximal years of schooling and immigrant status. Mathematics scores are normalized to have a mean of 0 and standard deviation of 1.

Figure 1 presents estimates of β_F , β_A and δ for sub-samples defined by parents' maximal years of education, allowing us to track the change in the gender gap with parental education separately for the Arabic and Hebrew sectors. It shows that the gap favoring girls in Hebrew-language schools, β_F , declines with parents' education, while the gap favoring girls in Arabic-language schools, $\beta_F + \delta$, increases with parental education. This is a key cultural difference between the Arabic- and Hebrew-language sectors.²³

5.3 Ethnic differences in gender gaps in twelfth-grade attainment

A similar picture emerges when estimating the ethnic difference in gender gaps with respect to twelfth-grade attainment measures using a linear probability model, presented in the top panel of Table 5.²⁴ As columns (1) show, the raw ethnic gap is substantial: girls in both language sectors have a higher probability of reaching twelfth grade and matriculating; and the gap favoring girls

²³Figure 1 can also be used to compare the ethnic gap for different levels of parental education, separately for male and female students: β_A , the ethnic gap among male students, increases (in absolute value) with parental education, where $\beta_A + \delta$, the ethnic gap among female students, shows no trend with parental education.

²⁴Full outputs for these regressions can be found in Table A4.

in Arabic-language schools, δ , is larger by about 10 percentage points than in Hebrew-language schools. Controlling for SES, in columns (2), does not alter the female advantage (β_F) or the ethnic difference in the female advantage (δ), but it does reduce the overall ethnic gap (β_A) by half, for retention, and by two-thirds, for matriculation rates. In columns (3) we add a second-degree polynomial of eighth-grade GEMS scores as well as an interaction term between mathematics and reading scores. Conditioned on eighth-grade scores and SES, the male retention and matriculation rates in Arabic schools are not significantly different from the corresponding rates in Hebrew-language schools, where the female rates in Arabic schools are significantly higher than in Hebrew-language schools. Gender gaps in both sectors, though reduced, remain significant after conditioning on prior scores and SES, as do the differences in the gender gap between the two language sectors. The advantage of girls over boys in Arabic schools grows during high school, and more so than the advantage of girls over boys in Hebrew-language schools.

Allowing the effect of socio-economic background to vary by gender in the bottom panel of Table 5 shows that the difference between Hebrew- and Arabic-language students in socio-economic composition explains 45 percent of the ethnic difference in the gender gap in retention, reduced from 0.11 to 0.06 (even more than in the case of GEMS scores), and leaves the estimated difference in matriculation rates unaltered. Allowing coefficients of both socio-economic status and prior achievement to vary by gender reduces the ethnic difference in gender gaps in retention by more than half, but increases by half the estimated ethnic difference in gender gaps in matriculation rates.

5.4 Ethnic differences in gender gaps in the choice of STEM electives

In Table 6 we estimate the ethnic difference in gender gaps in the choice of advanced science and mathematics matriculation electives for the entire study sample, using a linear probability model.²⁵ The top panel reveals that, as in previous outcomes, the differences between ethnic groups in the relative position of girls are persistent and statistically significant for all STEM choices, even af-

²⁵Full outputs for these regressions can be found in Table A5.

Table 5: Propensity for twelfth-grade attainment by gender or ethnicity, conditional on socio-economic indicators and prior achievement

	Twelfth-grade retention			Matriculation		
	(1)	(2)	(3)	(1)	(2)	(3)
	Difference in Difference					
Female, β_F	0.05*** (0.00)	0.06*** (0.00)	0.04*** (0.00)	0.12*** (0.01)	0.13*** (0.01)	0.07*** (0.00)
Arab, β_A	-0.13*** (0.03)	-0.07** (0.02)	-0.02 (0.02)	-0.27*** (0.02)	-0.08*** (0.02)	0.01 (0.01)
FemaleXArab, δ	0.11*** (0.02)	0.11*** (0.02)	0.07*** (0.02)	0.09*** (0.01)	0.09*** (0.01)	0.04*** (0.01)
	Ethnic gaps by gender (β_A^g)					
Females, β_A^F	-0.03* (0.01)	0.02 (0.01)	0.03*** (0.01)	-0.17*** (0.02)	0.01 (0.02)	0.06*** (0.02)
Males, β_A^M	-0.13*** (0.03)	-0.04 (0.02)	0.00 (0.02)	-0.27*** (0.02)	-0.08*** (0.02)	0.00 (0.01)
$\beta_A^F - \beta_A^M$	0.10	0.06	0.03	0.10	0.09	0.06
Controls						
SES		✓	✓		✓	✓
GEMS			✓			✓

Notes: In the top panel, $N = 68,050$; in the bottom panel $N_{female} = 33,799$ and $N_{male} = 34,251$. Dependent variables vary by column: Twelfth-grade retention; matriculation and matriculation. Coefficients are obtained from a LPM with school-level clustered standard errors and a dummy for cohort. In columns (2) and (3) estimates are conditioned on family income quintiles, parents' maximal years of schooling and immigrant status. In columns (3) estimates are also conditioned on a second degree orthogonalized polynomial of the four GEMS (mathematics, science, reading and English) as well as an interaction between the reading and mathematics percentiles. All GEMS scores are normalized to have a mean of 0 and standard deviation of 1. Standard errors in parentheses. * $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$

ter controlling for SES in columns (1). Conditioning choice on prior achievement in columns (2) slightly narrows the difference in gender gaps between the two language sectors, mainly due to the relatively low GEMS scores of Arab boys. After controlling for prior scores and SES, girls in Arabic-language schools are 2 percentage points less likely than boys to choose physics or computer science, a difference that is not statistically significant, compared to a highly significant 12 percentage point gap in Hebrew-language schools. Conditional on SES and prior achievement, there is no gender gap in advanced mathematics among Arab students while the underrepresentation of girls in Hebrew-language schools persists. Girls in both sectors are consistently more likely to choose advanced biology or chemistry, but more so in Arabic-language schools.

In columns (3) of Table 6 we add controls at the school level: school characteristics and electives offered in the school.²⁶ We construct school level controls from summary statistics based on the full population of twelfth-grade students, restricting the analysis to students enrolled in schools with at least 30 students from the full population.²⁷ School characteristics include: enrollment, share of female students, four-year or six-year school, school-level averages of GEMS scores and parental education, and the SES category of the school's municipality. Ayalon (2002) points to a difference between Arabic- and Hebrew-language schools in electives offered—fewer non-STEM matriculation electives in Arabic-language schools. To account for this we create a vector of dummy variables indicating whether at least 5% of students in the school took an advanced elective in the following categories: English, mathematics, physics or computer science, biology or chemistry, humanities, and other electives.²⁸

The results in columns (3) reveal that conditioning choice on school characteristics and electives offered does not alter the estimated ethnic difference in gender gaps for physics or computer

²⁶Including school fixed effects instead of observed characteristics yields similar results, available on request.

²⁷Removing dropouts from the sample reduces sample size to 60,967, and removing students attending schools with enrollment lower than 30 students further reduces the sample by 111 observations, to 60,856. Average enrollment per cohort in these years was 149 in Hebrew-language schools and 126 in Arabic-language schools.

²⁸We do not observe all electives in our data. We define schools as offering "other electives" if at least 5% of the students in a schools are eligible for a matriculation certificate—meaning that they have at least 21 units— but for whom we see in our observed electives less than 21 units. In the full population, 28.2% of students fit this criteria. The choice of the 5% minimum is to ensure we capture a subject offered in the schools, rather than individual students taking matriculation elective in an extracurricular format, which is common for subjects like music and dance that fall into the "other electives" category, but rare for the mainstream electives.

Table 6: Choice of advanced science and mathematics electives by gender, conditional on prior achievement and socio-economic status

	Physics or computer science			Advanced mathematics			Biology or chemistry		
	(1)	(2)	(3)	(1)	(2)	(3)	(1)	(2)	(3)
Difference in Difference									
Female, β_F	-0.10*** (0.01)	-0.12*** (0.00)	-0.13*** (0.00)	-0.02*** (0.00)	-0.04*** (0.00)	-0.04*** (0.00)	0.07*** (0.01)	0.04*** (0.01)	0.04*** (0.01)
Arab, β_A	-0.00 (0.01)	0.03*** (0.01)	0.02 (0.01)	0.03** (0.01)	0.07*** (0.01)	0.08*** (0.02)	0.19*** (0.02)	0.24*** (0.02)	0.17*** (0.03)
FemaleXArab, δ	0.12*** (0.01)	0.10*** (0.01)	0.10*** (0.01)	0.05*** (0.01)	0.04*** (0.01)	0.04*** (0.01)	0.12*** (0.01)	0.09*** (0.01)	0.07*** (0.01)
Ethnic gaps by gender (β_A)									
Female, β_A^F	0.09*** (0.01)	0.10*** (0.01)	0.09*** (0.02)	0.08*** (0.01)	0.10*** (0.01)	0.10*** (0.02)	0.34*** (0.02)	0.36*** (0.02)	0.25*** (0.03)
Male, β_A^M	0.02* (0.01)	0.06*** (0.01)	0.07*** (0.02)	0.03** (0.01)	0.07*** (0.01)	0.11*** (0.02)	0.17*** (0.02)	0.21*** (0.02)	0.16*** (0.02)
$\beta_A^F - \beta_A^M$	0.07	0.04	0.02	0.05	0.03	-0.01	0.17	0.15	0.09
Family SES	✓	✓	✓	✓	✓	✓	✓	✓	✓
GEMS		✓	✓		✓	✓		✓	✓
School ch.			✓			✓			✓
N	68,050	68,050	60,856	68,050	68,050	60,856	68,050	68,050	60,856
N_{female}	33,799	33,799	31,583	33,799	33,799	31,583	33,799	33,799	31,583
N_{male}	34,251	34,251	29,273	34,251	34,251	29,273	34,251	34,251	29,273

Notes: In the top panel, $N = 68,050$; in the bottom panel $N_{female} = 33,799$ and $N_{male} = 34,251$. Dependent variables vary by column: physics or computer science; advanced mathematics; and biology or chemistry. Coefficients are obtained from a LPM with school-level clustered standard errors and a dummy for cohort. In columns (1), estimates are conditioned on family income quintiles, parents' maximal years of schooling and immigrant status. In columns (2), estimates are also conditioned on a second degree orthogonalized polynomial of the four GEMS scores (mathematics, science, reading and English) as well as an interaction between the reading and mathematics percentiles. All GEMS scores are normalized to have a mean of 0 and standard deviation of 1. In columns (3) estimates are also conditioned on: school size, share of female students, four or six year school, school-level averages of GEMS scores, municipality SES, and indicators for the availability of matriculation elective categories. Standard errors in parentheses. * $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$

science and advanced mathematics. We do find that including these covariates significantly reduces the coefficient β_A and slightly reduces the ethnic difference in the gender gap δ , with regard to choosing biology or chemistry, indicating that differences in school characteristics and course offerings does explain to some extent differences between students in the two language sectors in choosing these science electives.²⁹

In the bottom panel of Table 6, we estimate equation (2) for male and female students separately. The difference in coefficients $\beta_A^F - \beta_A^M$ estimates the difference in gender gaps between Arabic- and Hebrew-language schools, allowing gender differences in the coefficients. After accounting for the different effects of SES and prior achievement by gender in columns (2), the gender gap in Arab schools remains significantly smaller by 4 percentage points in physics or computer science and by 3 percentage points in advanced mathematics, and larger by 15 percentage points in favor of girls in biology or chemistry. This implies that the differential effect of SES and prior achievement by gender accounts for 60 percent of the ethnic difference in the gender gap in physics or computer science and for a quarter of this difference in advanced mathematics. With respect to the choice of biology or chemistry, allowing slopes to vary by gender increases the estimated ethnic difference in the gender gap by two-thirds. In columns (3) allowing slopes on school characteristics to differ by gender further reduces the ethnic differences in gender gaps in physics or computer science and advanced mathematics. We cannot say whether this reflects sorting across schools or the effect of schools themselves.

5.5 Differences in the estimated gender gap for selected subsamples

Most analyses of gender gaps in the choice of STEM study tracks are based on samples of high school or college (bound) students (Turner and Bowen, 1999; Riegle-Crumb *et al.*, 2012; Arcidi-

²⁹We do not observe teachers' gender or teacher practices, which are likely to be important (Dee, 2007). With respect to the gender composition of the teaching staff, we note that in both language sectors the teaching staff is predominantly female, but more so in Hebrew-language high schools, and the share of women among physics teachers is higher in Hebrew-language schools, where gender gaps favoring boys are higher. Potential differences between language sectors in the gender bias of teaching practices are most likely a function of culture, as Arab teachers teach only in Arab schools, and *vice versa*.

acono, 2004; Arcidiacono and Koedel, 2013; Buser *et al.*, 2014; Reuben *et al.*, 2017). The prior selection implicit in these samples, especially samples of college students, suggests that their results may be biased with respect to population wide gender patterns.³⁰ Our main specification in Table 6 does not suffer from this bias as it estimates the ethnic difference in gender gaps using the full population of eighth-grade students, before students begin dropping out of school, with male dropout rates exceeding female dropout rates, and Arab male dropout rates exceeding all others.³¹ This is our preferred specification. Table 7 presents estimates of our coefficients of interest, β_F , β_A , and δ , for two alternative sample specifications, common in the literature, to facilitate comparisons to other studies: students enrolled in twelfth grade; and students eligible for a matriculation certificate (bound for tertiary education).

Limiting the sample to students enrolled in twelfth grade yields a slight increase in the relative propensity of Arab students to choose STEM matriculation subjects and a slight decrease in the propensity of female students to choose physics or computer science. The estimates of ethnic differences in gender gaps remain virtually unchanged, with a slight decrease of the difference in choosing biology or chemistry. Leaving dropouts out of the sample has the expected effect of improving the relative position of the group that suffers most from dropouts—male students in Arabic language schools—but it is a small effect. Significant differences arise when limiting the sample to students eligible for a matriculation certificate (college bound students). Here, the relative position of Arab students is dramatically improved, nearly doubled, in all choice categories, while estimated gender differences also increase—in favor of male students in physics or computer science and advanced mathematics, and in favor of female students in biology or chemistry. Conditional on matriculation, and our control variables, the two ethnic groups exhibit similar gender patterns in advanced mathematics and biology or chemistry—female students are 7 percentage points less likely to choose advanced mathematics and 6 percentage points more likely to choose biology or chemistry, compared to male students. However, even when restricting our analysis to matricu-

³⁰Fryer and Levitt (2010) discuss this type of selection with respect to the estimation of gender gaps in SAT scores, where the share of women tested is larger, so that the female sample draws more heavily from the middle of the ability distribution.

³¹In Israel, up to eighth grade, dropout rates are negligible, less than 1%.

Table 7: Difference-in-difference estimates for different subsamples

	Physics or computer science	Advanced mathematics	Biology or chemistry
Full study sample (N=68,050)			
Female, β_F	-0.12***	-0.04***	0.04***
Arab, β_A	0.03***	0.07***	0.24***
FemaleXArab, δ	0.10***	0.04***	0.09***
Students enrolled in twelfth grade (N=60,967)			
Female, β_F	-0.13***	-0.04***	0.04***
Arab, β_A	0.04***	0.08***	0.28***
FemaleXArab, δ	0.10***	0.04***	0.07***
Students eligible for matriculation certificate (N=37,843)			
Female, β_F	-0.20***	-0.07***	0.06***
Arab, β_A	0.09***	0.17***	0.42***
FemaleXArab, δ	0.11***	0.01	0.02

Notes: Dependent variables vary by column: choosing matriculation electives in physics or computer science; advanced mathematics; and biology or chemistry. Coefficients are obtained from a LPM with school-level clustered standard errors and a dummy for cohort. Estimates are conditioned on family income quintiles, parents' maximal years of schooling, immigrant status, a second degree orthogonalized polynomial of the four normalized GEMS scores (mathematics, science, reading and English) and an interaction between reading and mathematics percentiles. * $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$

lating students, the ethnic difference in the underrepresentation of women in physics or computer science persists.

6 Ethnic-gender differences in the marginal effect of prior achievement

As the choice models under uncertainty of Altonji (1993) and Arcidiacono (2004) highlight, test scores serve as a signal of ability for the student. Lower GEMS achievement levels are adverse signals, and previous research on gender differences in risk aversion and competitiveness suggests that boys are less deterred by adverse signals in choosing STEM subjects. In Friedman-Sokuler and Justman (2016) we found that the probability to choose any STEM elective increases in eighth-grade mathematics and science scores, but the slope was steeper for boys with regard to choosing advanced mathematics and physics or computer science, and steeper for girls with respect to choosing biology or chemistry. In section 5 we show that allowing the effect of prior achievement on the propensity to choose electives to vary by gender accounted for a substantial portion of the ethnic difference in gender gaps. In this section we examine whether gender differences in the effect of prior scores are similar across ethnic groups.

We begin by presenting the data graphically in Figure 2, which shows the propensity of choosing each of the three advanced STEM matriculation categories, by gender and language sector and by the percentile of achievement in GEMS mathematics. All twelve propensities increase in eighth-grade mathematics achievement but at different rates, depending on gender, ethnicity and subject category. These differences in the relationship between prior achievement and choice can explain some of the ethnic differences in gender gaps. In panel (a) of Figure 2, students in Hebrew-language schools exhibit a large gender gap in the propensity to choose physics or computer science which increases as a function of prior mathematics achievement, where we observe no such gender gap among students in Arabic-language schools. Gender and ethnic differences are smallest with respect to the propensity to choose advanced mathematics, in panel (b). However, where the male

propensity is slightly greater than the female propensity in Hebrew-language schools, the opposite is true in Arabic-language schools. With regard to the choice of biology and chemistry as a function of eighth-grade mathematics, in panel (c), we find a gender gap favoring female students in both language sectors, but larger in Arabic-language schools. All of this highlights the role of cultural conditioning in shaping the different response, by gender, to prior achievement.

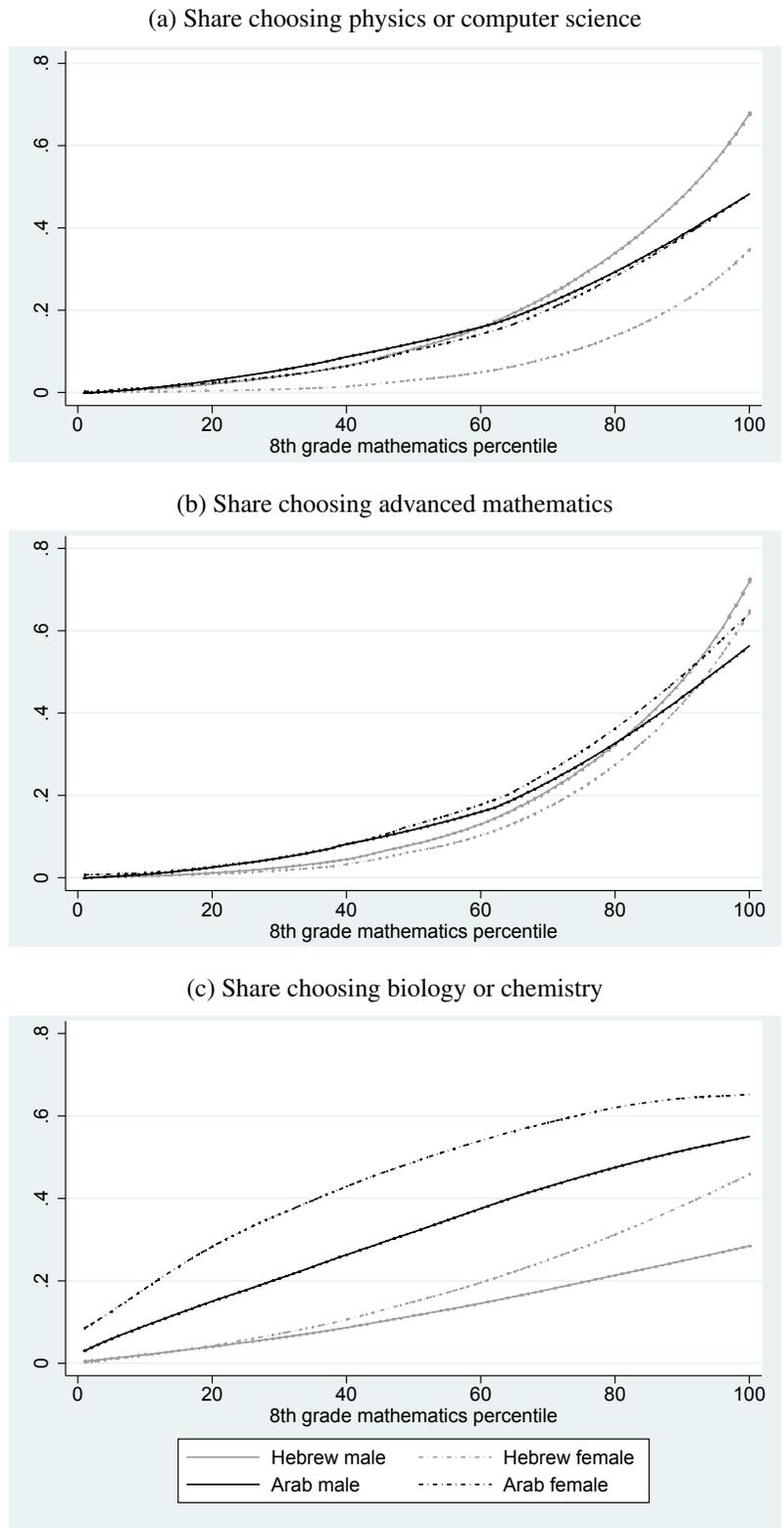
Table 8 quantifies this analysis for science electives, estimating the probability of choosing advanced science electives for each gender-language combination separately, conditional on socioeconomic status and polynomials of prior achievement.³² The regression results accord with the graphical analysis in Figure 2. For physics or computer science, we find no statistically significant gender differences in the response to prior achievement in Arabic-language schools and substantial differences by gender in Hebrew-language schools, where positive coefficients of prior scores are much larger for males than females. With respect to the choice of biology or chemistry, in Hebrew-language schools all the GEMS coefficients are positive and larger for female students, where in Arabic-language schools the marginal effect of mathematics achievement is twice as large for male students than for female students, while other coefficients are larger for female students. Moreover, for Arab female students, achievement in reading and English are stronger predictors for the choice of biology and chemistry than mathematics achievement. Arab girls who are good at mathematics go into physics or computer science or advanced mathematics, while those who are good students in general, but less so in mathematics, choose biology and chemistry.

7 Discussion

The previous sections established that differences in gender gaps in achievement between Hebrew- and Arabic-language schools are only partially explained by population differences in socioeconomic characteristics, and that differences in gendered choice patterns in matriculation are only partially accounted for by gaps favoring Arab girls in eighth-grade achievement. The find-

³²We focus on science matriculation electives in Table 8, omitting advanced mathematics for brevity. Science electives exhibit larger gender and ethnic differences. Results for advanced mathematics are available upon request.

Figure 2: Share choosing science electives by gender and language sector, by eighth-grade mathematics and reading scores



Notes: Graphs represent share of students tested in each matriculation elective, by eighth-grade mathematics achievement percentiles. Percentiles are defined over the whole population. Lines are smoothed using Stata's Lowess procedure for kernel-weighted local polynomial smoothing 28

Table 8: Choice of advanced science and mathematics electives estimated separately by gender-ethnic groups, conditional on prior achievement and socio-economic status

	Physics or computer science				Biology or chemistry			
	Hebrew		Arabic		Hebrew		Arabic	
	Male	Female	Male	Female	Male	Female	Male	Female
GEMS								
Mathematics	0.09*** (0.00)	0.04*** (0.00)	0.07*** (0.01)	0.06*** (0.01)	0.03*** (0.00)	0.06*** (0.00)	0.07*** (0.01)	0.03* (0.02)
Science	0.04*** (0.00)	0.02*** (0.00)	0.02*** (0.01)	0.02*** (0.01)	0.03*** (0.00)	0.05*** (0.00)	0.04** (0.01)	0.05*** (0.01)
Reading	0.03*** (0.00)	0.01** (0.00)	0.05*** (0.01)	0.05*** (0.01)	0.02*** (0.00)	0.03*** (0.00)	0.08*** (0.01)	0.09*** (0.01)
English	0.02*** (0.00)	0.00** (0.00)	0.03*** (0.01)	0.02*** (0.01)	0.02*** (0.00)	0.02*** (0.00)	0.01 (0.01)	0.05*** (0.01)
Mathematics X Reading	0.03*** (0.00)	0.01*** (0.00)	0.03*** (0.01)	0.03*** (0.01)	0.01** (0.00)	0.02*** (0.00)	0.02** (0.01)	-0.01 (0.01)
GEMS ²								
Mathematics	0.06*** (0.00)	0.04*** (0.00)	0.02** (0.01)	0.03*** (0.01)	0.00 (0.00)	0.01** (0.00)	-0.01 (0.01)	-0.02 (0.01)
Science	0.02*** (0.00)	0.01*** (0.00)	0.02*** (0.00)	0.01* (0.01)	0.02*** (0.00)	0.02*** (0.00)	0.01 (0.01)	0.00 (0.01)
Reading	0.01** (0.00)	0.00 (0.00)	0.01 (0.01)	0.02*** (0.00)	0.00 (0.00)	0.01 (0.00)	-0.02* (0.01)	0.00 (0.01)
English	0.01*** (0.00)	0.00 (0.00)	0.01* (0.00)	0.01* (0.00)	0.01*** (0.00)	0.01*** (0.00)	0.01* (0.01)	0.02* (0.01)
Constant	0.11*** (0.01)	0.03*** (0.01)	0.14*** (0.01)	0.10*** (0.01)	0.09*** (0.01)	0.10*** (0.01)	0.29*** (0.02)	0.42*** (0.03)
Observations	26,061	25,529	8,190	8,270	26,061	25,529	8,190	8,270
R-squared	0.299	0.146	0.226	0.214	0.092	0.144	0.184	0.196

Notes: Dependent variables vary by column: choosing physics or computer science; advanced mathematics; and biology or chemistry. Coefficients are obtained from a LPM conditional on parents' maximal years of education and family income quintiles, with school-level clustered standard errors and a dummy for cohort and immigrant. All GEMS scores are normalized to have a mean of 0 and standard deviation of 1. Standard errors in parentheses. * $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$

ing that girls in the ethnic group with *less* gender equality perform *better* and take *more* STEM majors accords with Fryer and Levitt's 2010 findings on the mathematics gap favoring girls in Arab (Muslim) countries. It indicates that this pattern is persistent across contexts and is not limited to achievement on international exams, but also extends to the choice of STEM matriculation outcomes.

Both in Israel and in the Arab world, these patterns are not reflected in the labor market. In Israel, the Arab female labor force participation rate is 28%, much lower than for Arab men and Jewish women, 64% and 66% respectively (Central Bureau for Statistics, 2015). This low participation rate is similar to those of women in other Arab countries (Yashiv and Kasir, 2015). Arab women in Israel are often employed in occupations that do not require a matriculation certificate or tertiary qualifications in STEM subjects, such as personal care and sales, which account for 43% of the Arab women in the labor force (Central Bureau for Statistics, 2013, Table 2.17). Among those in professional occupations, the under-representation of women relative to men in science, engineering and IT occupations is similar in both ethnic groups.³³ Even within the teaching profession, the second largest category of employment among Arab women, female teachers constitute 73% of all Arab teaching professionals, but only 26% of physics teachers in Arab schools, compared to 40% in Hebrew schools (Knesset Research and Information Center, 2012).³⁴ However, Arab society in Israel is undergoing a cultural shift towards modernity, as are many countries in the Middle East and North Africa, a shift reflected in, among other things, the reversal of the overall gender gap in education (Bossavie and Kanninen, 2018). Current gendered patterns in the labor market may not yet reflect the changes taking place within younger cohorts.

Akerlof and Kranton (2000), in explaining occupational gender segregation, and the earlier sorting into study fields, emphasize the notion that specific occupations are associated with the social categories "man" and "woman". Nosek *et al.* (2009), using implicit association tests, iden-

³³Only 1% of Arab women are science and engineering or IT professionals, compared to 3% of Arab men, 5% of Jewish women and 10% of Jewish men (Central Bureau for Statistics, 2013, Table 2.17).

³⁴Almost all teachers in Arab schools are Arabs and all teachers in Hebrew schools are Jews or other. Similar ethnic differences in gender gaps are found in chemistry and biology where about half of the teachers in Arabic schools are female compared to more than 80% in Hebrew schools.

tify systematic variation across 34 countries in implicit attitudes associating men with science more than women, and show that this gender bias strongly correlates with nation-wide male-to-female achievement gaps in eighth-grade TIMSS science and mathematics scores, but not with self-reported stereotypes. Nosek *et al.* (2009) find that Hebrew speaking participants from Israel exhibit above-average implicit gender bias,³⁵ while countries such as Jordan and Iran exhibit below-average levels of implicit stereotypes. These findings indicate the presence of cultural differences in the association between science and gender which are independent of cultural differences regarding overall gender equality. This suggests that as the share of Arab women in the labor market increases the share of Arab women in STEM occupations may also increase.³⁶

At the same time, there are also indications that marriage market incentives act as cultural mechanisms that induce investment in education and human capital, which may not necessarily translate into increased female participation in the labor force in STEM occupations. Prior evidence indicates that investment in the education of young women in traditional societies is related to their prospects in the marriage market (Hu and Schlosser, 2015; Ashraf *et al.*, 2016). In this vein, Read and Cohen (2007) analyze United States Census data and find that the link between education and employment is inconsistent across ethnic groups—the combination of high education and low employment is evident among Arab, Iranian, Korean, and Asian Indian women. Ethnographic studies of Arab women in Israel and the United States provide further support, finding that because women in Arab society are responsible for the socialization and education of their children to a greater extent than women in Western societies, their own education is valued more as a resource for the home than as an asset in the labor market (Sa’ar, 2006; Read and Oselin, 2008).

Finally, educational attainment and achievement also plays a role in the empowerment of women in Arab society in Israel. Sabbah-Karkaby and Stier (2017) examined marital behavior in Arab society in Israel with relation to educational attainment. They find that the increase in female education changed the link between education and age at marriage. While young age is

³⁵The sample from Israel did not cover the Arab minority

³⁶The limited supply of jobs in the largest occupation for educated Arab women—teaching—may also contribute to this trend (Zur, 2017).

considered an asset in the marriage market, higher education is becoming more important over time, and in particular allows postponement of marriage. However, the pursuit of post-secondary education still requires the consent of the men in their families, which is conditioned on proof of ability and high levels of achievement in secondary education (Seginer and Vermulst, 2002). This provides added incentive for Arab girls to take on challenging matriculation electives, such as physics and advanced mathematics, to prove their potential. Currently most do not persist in these fields into tertiary education and the labor market but the potential is there.

8 Concluding remarks

In this paper we point to the role of culturally conditioned gender norms in shaping gender gaps in educational achievement and choice. We do so by comparing two distinct ethno-linguistic groups, Hebrew and Arabic speakers, attending separate coeducational schools within the highly centralized Israeli education system. In eighth-grade achievement, students in Hebrew-language schools outperform those in Arabic-language schools, and girls outperform boys. In line with the findings of Fryer and Levitt (2010), we show that, in middle school, the advantage of girls over boys in mathematical achievement in the predominantly Muslim, Arabic-language sector, characterized by patriarchal-traditional cultural norms, is greater than in the predominantly Jewish, Hebrew-language sector characterized by western-egalitarian gender norms. We find that the lower level of SES of the Arab population accounts for about half of the gap in favour of Jewish students, but explains only a small fraction of the difference in gender gaps.

We extend these finding to twelfth-grade attainment and matriculation choices. We find that retention and matriculation rates are higher for students in Hebrew-language schools than for students in Arabic-language schools; higher for female students than for male students; and that the gender gap favoring females is *larger* in Arabic-language schools. We find that differences in SES and prior achievement account for the entire gap between language sectors, and reduce gender gaps by 30-50%. A more complex picture emerges with respect to the choice of STEM matricula-

tion electives. Students in Arabic-language schools choose biology and chemistry at higher rates than students in Hebrew-language schools while the opposite is true for advanced mathematics, computer science and to a lesser extent physics. Gender patterns with respect to the latter three subject differ between language sectors—Arab girls are slightly overrepresented in advanced mathematics and physics, while girls in Hebrew-language schools are significantly under-represented. Moreover, while in Hebrew-language the gender gaps favoring men in physics, computer science and advanced mathematics electives schools increases in early mathematical achievement, in Arabic-language schools gender gaps favoring men are non-existent and even reversed among top achieving students.

This inverse relationship between societal levels of gender equality and gender equality in STEM related educational outcomes, suggests that culture, manifested in gender norms, is not a single factor but rather a multiplicity of forces shaping educational outcomes. Our reading of the literature, suggest three such channels operating in the Israeli context. First, from an identity perspective, the stereotype that associates science with masculinity, which contributes to the persistence of gender gaps in Western societies, is much weaker in Arab society. Second, cultural differences in gender norms yields larger returns to female education in the Arab marriage market. Third, the patriarchal structure of Arab society provides added incentive for Arab girls to excel in mathematically intensive fields, to signal their academic potential to their family and gain access to higher education. These channels, while context specific, point to the need to widen the perspective through which we understand the ways in which culture and norms shape gender gaps in education and in the labor market.

From a policy perspective, these findings suggest different approaches to promoting female participation in STEM occupations for each ethnic group. The relatively large share of Arab women completing high school with qualifications that allow them to continue to mathematically intensive tertiary degrees such as IT and engineering, suggests that policy measures in this sector should focus on the transition from secondary to tertiary education, and on fostering opportunities in the labor market. In the Hebrew-language sector, where women are already under-represented in sci-

ence and mathematics in secondary school, our analysis points to the need to identify and address societal and normative structures that shape gender streaming at earlier stages in the educational pipeline.

References

- Abu-Baker, K. (1998) On an unpaved road: Arab women as political leaders in Israel, in *Modern Welfare and Tradition: Palestinian Women in Israel Coping with Changes in their Life Settings* (Ed.) A. Manna, Van Leer Institute and Kibbutz Meuchad Publishers, Jerusalem.
- Abu-Baker, K. and Azaiza, F. (2010) Strategies for closing the educational gaps among Palestinian couples in Israel, *Hawwa*, **8**, 154–180.
- Akerlof, G. A. and Kranton, R. E. (2000) Economics and identity, *The Quarterly Journal of Economics*, **115**, 715–753.
- Altonji, J. G. (1993) The demand for and return to education when education outcomes are uncertain, *Journal of Labor Economics*, **11**, pp. 48–83.
- Antecol, H. (2000) An examination of cross-country differences in the gender gap in labor force participation rates, *Labour Economics*, **7**, 409 – 426.
- Arcidiacono, P. (2004) Ability sorting and the returns to college major, *Journal of Econometrics*, **121**, 343 – 375.
- Arcidiacono, P. and Koedel, C. (2013) Race and college success: Evidence from Missouri, Working Paper 19188, National Bureau of Economic Research.
- Ashraf, N., Bau, N., Nunn, N. and Voena, A. (2016) Bride price and female education, Working Paper 22417, National Bureau of Economic Research.
- Ayalon, H. (2002) Mathematics and sciences course taking among Arab students in Israel: A case of unexpected gender equality, *Educational Evaluation and Policy Analysis*, **24**, 63–80.

- Benavot, A. and Resh, N. (2003) Educational governance, school autonomy, and curriculum implementation: A comparative study of Arab and Jewish schools in Israel, *Journal of Curriculum Studies*, **35**, 171–196.
- Birenbaum, M. and Nasser, F. (2006) Ethnic and gender differences in mathematics achievement and in dispositions towards the study of mathematics, *Learning and Instruction*, **16**, 26 – 40.
- Birenbaum, M., Nasser, F. and Tatsuoka, C. (2007) Effects of gender and ethnicity on fourth graders' knowledge states in mathematics, *International Journal of Mathematical Education in Science and Technology*, **38**, 301–319.
- Blass, N., Tsur, S. and Zussman, N. (2010) The allocation of teachers' working hours in primary education, 2001–09, Working Paper 2010.18, Research Department, Bank of Israel.
- Blau, F. D. and Kahn, L. M. (2017) The gender wage gap: Extent, trends, and explanations, *Journal of Economic Literature*, **55**, 789–865.
- Bossavie, L. and Kanninen, O. (2018) What explains the gender gap reversal in education? The role of the tail hypothesis, Working Paper 8303, World Bank.
- Buser, T., Niederle, M. and Oosterbeek, H. (2014) Gender, competitiveness, and career choices, *The Quarterly Journal of Economics*, **129**, 1409–1447.
- Ceci, S. J., Ginther, D. K., Kahn, S. and Williams, W. M. (2014) Women in academic science: A changing landscape, *Psychological Science in the Public Interest*, **15**, 75–141.
- Central Bureau for Statistics (2003) Statistical Abstract of Israel, http://www.cbs.gov.il/reader/shnatonhnew_site.htm.
- Central Bureau for Statistics (2013) Labor Force Survey of Israel, http://www.cbs.gov.il/reader/y_labor/yearm_h_new.htm?CYear_co=2007#6.
- Central Bureau for Statistics (2015) Statistical Abstract of Israel, http://www.cbs.gov.il/reader/shnatonhnew_site.htm.

- Cinamon, R. G. (2009) Role salience, social support, and work—family conflict among Jewish and Arab female teachers in Israel, *Journal of Career Development*, **36**, 139–158.
- Dee, T. S. (2007) Teachers and the gender gaps in student achievement, *The Journal of Human Resources*, **42**, 528–554.
- DiPrete, T. A. and Jennings, J. L. (2012) Social and behavioral skills and the gender gap in early educational achievement, *Social Science Research*, **41**, 1 – 15.
- Dwairy, M. (1997) *Personality, culture, and Arab society*, Al Noor Press.
- Dwairy, M. (2004) Parenting styles and mental health of Palestinian–Arab adolescents in Israel, *Transcultural Psychiatry*, **41**, 233–252.
- Dwyer, R. E., Hodson, R. and McCloud, L. (2013) Gender, debt, and dropping out of college, *Gender & Society*, **27**, 30–55.
- Feniger, Y. (2010) The gender gap in advanced math and science course taking: Does same-sex education make a difference?, *Sex Roles*, **65**, 670–679.
- Fernández, R. (2011) Does culture matter?, North-Holland, vol. 1 of *Handbook of Social Economics*, pp. 481 – 510.
- Fernández, R. and Fogli, A. (2006) Fertility: The role of culture and family experience, *Journal of the European Economic Association*, **4**, 552–561.
- Fernández, R. and Fogli, A. (2009) Culture: An empirical investigation of beliefs, work, and fertility, *American Economic Journal: Macroeconomics*, **1**, 146–177.
- Fogiel-Bijaoui, S. (2002) Familism, postmodernity and the state: The case of Israel, *Journal of Israeli History*, **21**, 38–62.
- Friedman-Sokuler, N. and Justman, M. (2016) Gender streaming and prior achievement in high school science and mathematics, *Economics of Education Review*, **53**, 230 – 253.

- Fryer, R. G. and Levitt, S. D. (2010) An empirical analysis of the gender gap in mathematics, *American Economic Journal: Applied Economics*, **2**, pp. 210–240.
- Gharrah, R. (2015) Arab Society in Israel (7): Population, Society, Economy, <http://www.vanleer.org.il/he/content/%D7%A1%D7%A4%D7%A8-%D7%94%D7%97%D7%91%D7%A8%D7%94-%D7%94%D7%A2%D7%A8%D7%91%D7%99%D7%AA-%D7%91%D7%99%D7%A9%D7%A8%D7%90%D7%9C-%D7%A9%D7%A0%D7%AA%D7%95%D7%9F-%D7%A1%D7%98%D7%98%D7%99%D7%A1%D7%98%D7%99>.
- Goldin, C., Katz, L. F. and Kuziemko, I. (2006) The homecoming of American college women: The reversal of the college gender gap, *The Journal of Economic Perspectives*, **20**, 133–156.
- Guiso, L., Monte, F., Sapienza, P. and Zingales, L. (2008) Culture, gender, and math, *Science*, **320**, 1164–1165.
- Hu, L. and Schlosser, A. (2015) Prenatal sex selection and girls' well-being: Evidence from India, *The Economic Journal*, **125**, 1227–1261.
- Justman, M. (2014) Differential budgeting in education: Agreement in principle, difficulties in implementation (Hebrew), prepared for Eli Hurvitz Conference on Economy and Society, The Van Leer Jerusalem Institute.
- Justman, M. and Méndez, S. J. (2018) Gendered choices of STEM subjects for matriculation are not driven by prior differences in mathematical achievement, *Economics of Education Review*, *forthcoming*.
- Kalekin-Fishman, D. (2004) *Ideology, Policy, and Practice: Education for Immigrants and Minorities in Israel Today*.
- Knesset Research and Information Center (2012) Statistics on teaching staff in science and technology, <https://www.knesset.gov.il/mmm/data/pdf/m03089.pdf>.

- Lavy, V. (1998) Disparities between Arabs and Jews in school resources and student achievement in Israel, *Economic Development and Cultural Change*, **47**, pp. 175–192.
- Nollenberger, N., Rodríguez-Planas, N. and Sevilla, A. (2016) The math gender gap: The role of culture, *American Economic Review*, **106**, 257–61.
- Nosek, B. A., Smyth, F. L., Sriram, N., Lindner, N. M., Devos, T., Ayala, A., Bar-Anan, Y., Bergh, R., Cai, H., Gonsalkorale, K., Kesebir, S., Maliszewski, N., Neto, F., Olli, E., Park, J., Schnabel, K., Shiomura, K., Tulbure, B. T., Wiers, R. W., Somogyi, M., Akrami, N., Ekehammar, B., Vianello, M., Banaji, M. R. and Greenwald, A. G. (2009) National differences in gender–science stereotypes predict national sex differences in science and math achievement, *Proceedings of the National Academy of Sciences*, **106**, 10593–10597.
- OECD (2016) Education policy outlook country profile: Israel, <http://www.oecd.org/israel/Education-Policy-Outlook-Country-Profile-Israel.pdf>.
- Oyserman, D. (1993) The lens of personhood: Viewing the self and others in a multicultural society, *Journal of Personality and Social Psychology*, **65**, 993 – 1009.
- Rapoport, B. and Thibout, C. (2018) Why do boys and girls make different educational choices? The influence of expected earnings and test scores, **62**, 205–229.
- Rapp, J. (2015) Gender gaps in mathematics and language in Israel– What can be learned from the Israeli case?, Working paper, National Authority for Measurement and Evaluation in Education.
- Read, J. G. and Cohen, P. N. (2007) One size fits all? Explaining U.S.-born and immigrant women’s employment across 12 ethnic groups, *Social Forces*, **85**, 1713–1734.
- Read, J. G. and Oselin, S. (2008) Gender and the education-employment paradox in ethnic and religious contexts: The case of Arab Americans, *American Sociological Review*, **73**, 296–313.
- Reuben, E., Wiswall, M. and Zafar, B. (2017) Preferences and biases in educational choices and

- labour market expectations: Shrinking the black box of gender, *The Economic Journal*, **127**, 2153–2186.
- Riegle-Crumb, C., King, B., Grodsky, E. and Muller, C. (2012) The more things change, the more they stay the same? Prior achievement fails to explain gender inequality in entry into fSTEM college majors over time, *American Educational Research Journal*, **49**, 1048–1073.
- Sa'ar, A. (2006) Feminine strength: Reflections on power and gender in Israeli-Palestinian culture, *Anthropological Quarterly*, **79**, 397–430.
- Sabbah-Karkaby, M. and Stier, H. (2017) Links between education and age at marriage among Palestinian women in Israel: Changes over time, *Studies in Family Planning*, **48**, 23–38.
- Seginer, R. and Vermulst, A. (2002) Family environment, educational aspirations, and academic achievement in two cultural settings, *Journal of Cross-Cultural Psychology*, **33**, 540–558.
- Shir, T. (2014) Gender segregation in Hebrew state religious primary schools, Working Paper 2014.06, Research Department, Bank of Israel.
- Turner, S. E. and Bowen, W. G. (1999) Choice of major: The changing (unchanging) gender gap, *Industrial and Labor Relations Review*, **52**, 289 – 313.
- United Nations Economic Commission for Europe (2015) Indicators of Gender Equality, <http://http://www.unece.org/index.php?id=38461&L=0>.
- Yashiv, E. and Kasir, N. (2011) Patterns of labor force participation among israeli arabs, *Israel Economic Review*, **9**.
- Yashiv, E. and Kasir, N. (2015) The labour market of Israeli Arabs: Key features and policy solutions, Policy Insight 78, Centre for Economic Policy Research.
- Zur, Y. (2017) 11,000 Arab teachers in Israel unemployed while Jewish schools face teacher shortage, *Haaretz*, <https://www.haaretz.com/israel-news/>

11k-arab-teachers-unemployed-as-jewish-schools-face-teacher-shortage-1.
5628951.

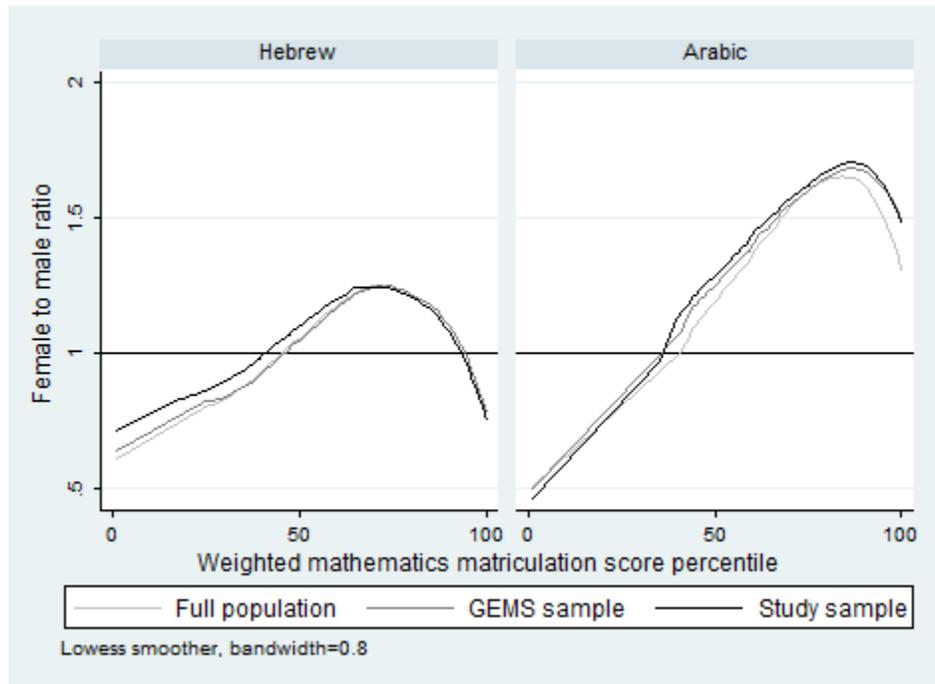
A1 Attrition

Figure A1 graphically compares female to male ratios by percentile of twelfth-grade mathematics matriculation scores across samples. In both language sectors and in all samples the patterns of gender ratios are nearly identical: girls in Hebrew language schools are under-represented in the top decile of mathematical achievement, while Arabic girls are substantially over-represented. In Arabic-language schools, the high end of the score distribution is affected by the omission of Arabic Church schools from the GEMS and study sample, but this has little effect on the ethnic differences in gender ratios. The right-hand column of Table A1 compares ethnic differences in gender gaps in 12th grade attainment and choice rates between the full population and the study sample, numerically. As in the case of mathematics scores, attrition between the full population and the study sample has little effect on these ethnic differences.

Table A1: Sectoral differences in gender gaps in twelfth-grade attainment and subject choice, in the full population and the study sample

	Arabic-language schools			Hebrew-language schools			Overall (g) (c)/(f)
	F/M ratio			F/M ratio			
	(a) Population	(b) Study	(c) (a)/(b)	(d) Population	(e) Study	(f) (d)/(e)	
Reached 12th grade	1.27	1.21	1.05	1.09	1.06	1.03	1.02
Matriculated	1.86	1.77	1.05	1.29	1.22	1.06	0.99
Physics or computer science	1.10	1.16	0.95	0.41	0.41	1.00	0.95
Advanced mathematics	1.40	1.43	0.98	0.91	0.88	1.03	0.95
Biology or chemistry	1.91	1.83	1.04	1.55	1.50	1.03	1.01

Figure A1: Female to male ratio in achievement percentile of weighted mathematics matriculation scores, by language sector and sample using Lowess smoothing



Matriculation mathematics exams are identical across language sectors, and students choose if to take the mathematics matriculation exam and the difficulty level of the test. To account for differences in the level of difficulty we construct a unified matriculation mathematics score that follows the weighting system used to determine university admissions in Israel—25 point bonus for 5 units, 15 point bonus for 4 units and no bonus for 3 units. For students taking 1 unit of mathematics (not enough for full matriculation, and therefore not enough to gain admission to university) we deduct 50 points (with a lower bound of 0); and we assign 0 points to students not taking any matriculation mathematics test. Students are then sorted into achievement percentiles, separately for Hebrew- and Arabic-language schools, in which the lowest percentile is relatively large, containing 28% of the full population, leaving empty the following percentiles.

Table A2: Sample composition and attrition

GEMS sample							
Hebrew schools				Arabic schools			
# of GEMS	Female	Male		Female	Male		
0	10%	12%		11%	14%		
1	2%	3%		1%	3%		
2	7%	8%		4%	6%		
3	23%	23%		15%	17%		
4	58%	54%		68%	59%		
N	30,690	32,669		10,529	11,124		
	63,359			21,653			
	85,012						
	Hebrew schools			Arabic schools			Ethnic gap
	Female	Male	Gender gap	Female	Male	Gender gap	
Mathematics GEMS	53.47 (23.48)	51.62 (24.92)	0.08	40.81 (22.25)	35.03 (22.58)	0.23	0.59
Science GEMS	64.81 (18)	63.93 (20.36)	0.04	58.38 (19.78)	50.66 (22.55)	0.38	0.48
Reading GEMS	67.49 (18.36)	58.93 (20.78)	0.39	55.16 (21.96)	41.38 (23.06)	0.63	0.68
English GEMS	81.59 (19.09)	76.65 (22.6)	0.21	65.25 (21.45)	55.72 (24.57)	0.41	0.80
Study sample							
Hebrew schools				Arabic schools			
# of GEMS	Female	Male		Female	Male		
2	8%	9%		4%	7%		
3	26%	27%		17%	20%		
4	66%	64%		79%	73%		
N	25529	26061		8270	8190		
	51,590			16,460			
	68,050						
	Hebrew schools			Arabic schools			Ethnic gap
	Female	Male	Gender gap	Female	Male	Gender gap	
Mathematics GEMS	53.75 (23.33)	52.11 (24.79)	0.07	41.61 (22.22)	35.81 (22.51)	0.24	0.58
Science GEMS	65.00 (17.82)	64.28 (20.15)	0.04	59.22 (19.57)	51.7 (22.32)	0.38	0.46
Reading GEMS	67.91 (18.01)	59.52 (20.48)	0.39	56.00 (21.83)	42.54 (22.91)	0.62	0.67
English GEMS	81.92 (18.75)	77.16 (22.2)	0.21	66.12 (21.23)	57.11 (24.08)	0.40	0.79

Gender gap= (female average-male average)/sample standard deviation; ethnic gap= (Hebrew average-Arabic average)/sample standard deviation

A2 Regression outputs

Table A3: Eighth-grade GEMS scores, conditioned on gender, ethnicity and socio-economic indicators

	Mathematics		Science		Reading		English	
Female	0.07*** (0.01)	0.08*** (0.01)	0.04** (0.01)	0.05*** (0.01)	0.38*** (0.01)	0.39*** (0.01)	0.20*** (0.01)	0.21*** (0.01)
Arab	-0.66*** (0.04)	-0.27*** (0.04)	-0.62*** (0.04)	-0.27*** (0.04)	-0.77*** (0.04)	-0.43*** (0.04)	-0.86*** (0.05)	-0.46*** (0.05)
Female X Arab	0.17*** (0.03)	0.16*** (0.02)	0.34*** (0.03)	0.33*** (0.02)	0.23*** (0.02)	0.23*** (0.02)	0.18*** (0.02)	0.18*** (0.02)
Family income quintiles								
2nd		0.07*** (0.02)		0.08*** (0.01)		0.09*** (0.01)		0.07*** (0.01)
3rd		0.13*** (0.02)		0.14*** (0.02)		0.14*** (0.02)		0.13*** (0.02)
4th		0.24*** (0.02)		0.25*** (0.02)		0.26*** (0.02)		0.23*** (0.02)
5th		0.42*** (0.02)		0.37*** (0.02)		0.41*** (0.02)		0.40*** (0.02)
Immigrant		0.09** (0.03)		-0.03 (0.02)		-0.21*** (0.02)		0.08*** (0.02)
Parents' maximal years of schooling								
12 years		0.24*** (0.02)		0.26*** (0.02)		0.29*** (0.02)		0.28*** (0.02)
13-15 years		0.51*** (0.02)		0.51*** (0.02)		0.52*** (0.02)		0.56*** (0.02)
16 years or more		0.67*** (0.02)		0.63*** (0.02)		0.66*** (0.02)		0.71*** (0.02)
Constant	0.05 (0.03)	-0.56*** (0.03)	0.24*** (0.02)	-0.34*** (0.03)	-0.06* (0.02)	-0.65*** (0.03)	-0.03 (0.03)	-0.67*** (0.03)
Observations	61,064	61,064	60,157	60,157	62,429	62,429	61,210	61,210
R-squared	0.074	0.166	0.062	0.140	0.138	0.233	0.156	0.255

Notes: Dependent variables vary by column and are standardized GEMS scores. Coefficients are obtained from a linear regression model with school-level clustered standard errors and a dummy for cohort. Family SES variables include family income quintiles, parents' maximal years of schooling and immigrant status. Standard errors in parentheses.

* $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$

Table A4: Propensity for twelfth-grade attainment, conditional on gender, ethnicity and socio-economic indicators and prior achievement

	Twelfth-grade retention			Matriculation		
Female	0.05*** (0.00)	0.06*** (0.00)	0.04*** (0.00)	0.12*** (0.01)	0.13*** (0.01)	0.07*** (0.00)
Arab	-0.13*** (0.03)	-0.07** (0.02)	-0.02 (0.02)	-0.27*** (0.02)	-0.08*** (0.02)	0.01 (0.01)
Female X Arab	0.11*** (0.02)	0.11*** (0.02)	0.07*** (0.02)	0.09*** (0.01)	0.09*** (0.01)	0.04*** (0.01)
Family income quintiles						
2nd		0.03*** (0.01)	0.02*** (0.01)		0.04*** (0.01)	0.02*** (0.01)
3rd		0.07*** (0.01)	0.05*** (0.01)		0.09*** (0.01)	0.05*** (0.01)
4th		0.09*** (0.01)	0.06*** (0.01)		0.16*** (0.01)	0.09*** (0.01)
5th		0.11*** (0.01)	0.07*** (0.01)		0.25*** (0.01)	0.14*** (0.01)
Immigrant		-0.06*** (0.01)	-0.05*** (0.01)		-0.05*** (0.01)	-0.04*** (0.01)
Parents' maximal years of schooling						
12 years		0.07*** (0.01)	0.04*** (0.01)		0.13*** (0.01)	0.06*** (0.01)
13-15 years		0.09*** (0.01)	0.04*** (0.01)		0.25*** (0.01)	0.10*** (0.01)
16 years or more		0.09*** (0.01)	0.03*** (0.01)		0.31*** (0.01)	0.12*** (0.01)
GEMS						
Mathematics			0.02*** (0.00)			0.09*** (0.00)
Science			0.02*** (0.00)			0.04*** (0.00)
Reading			0.03*** (0.00)			0.08*** (0.00)
English			0.02*** (0.00)			0.05*** (0.00)
Mathematics X Reading			-0.00 (0.00)			0.01* (0.00)
GEMS ²						
Mathematics ²			-0.00* (0.00)			-0.01*** (0.00)
Science ²			-0.01*** (0.00)			0.01** (0.00)
Reading ²			-0.02*** (0.00)			0.00 (0.00)
English ²			-0.01 (0.00)			0.02*** (0.00)
Constant	0.89*** (0.01)	0.76*** (0.01)	0.82*** (0.01)	0.55*** (0.01)	0.25*** (0.01)	0.40*** (0.01)
R-squared	0.035	0.073	0.142	0.059	0.158	0.321

Notes: $N_{total} = 68,050$. Dependent variables vary by column; Twelfth-grade retention; matriculation; and matriculation meeting university requirements. Coefficients are obtained from a LPM with school-level clustered standard errors and a dummy for cohort. All GEMS scores are normalized to have a mean of 0 and standard deviation of 1. Standard errors in parentheses. * $p < 0.05$
** $p < 0.01$ *** $p < 0.001$

Table A5: Choice of advanced science and mathematics electives, conditional on gender, ethnicity, prior achievement and socio-economic status

	Physics or computer science				Advanced mathematics				Biology or chemistry			
Female	-0.11*** (0.01)	-0.10*** (0.01)	-0.12*** (0.00)	-0.12*** (0.00)	-0.02*** (0.00)	-0.02*** (0.00)	-0.04*** (0.00)	-0.04*** (0.00)	0.06*** (0.01)	0.07*** (0.01)	0.04*** (0.01)	0.04*** (0.01)
Arab	-0.10*** (0.01)	-0.00 (0.01)	0.03*** (0.01)	0.02 (0.05)	-0.08*** (0.01)	0.03** (0.01)	0.07*** (0.01)	0.00 (0.04)	0.09*** (0.02)	0.19*** (0.02)	0.24*** (0.02)	0.05 (0.03)
Female X Arab	0.12*** (0.01)	0.12*** (0.01)	0.10*** (0.01)	0.10*** (0.01)	0.06*** (0.01)	0.05*** (0.01)	0.04*** (0.01)	0.04*** (0.01)	0.12*** (0.01)	0.12*** (0.01)	0.09*** (0.01)	0.06*** (0.01)
Family income quintiles												
2nd		0.01*** (0.00)	0.01* (0.00)	0.00 (0.00)		0.01*** (0.00)	0.01 (0.00)	0.00 (0.00)		0.03*** (0.01)	0.02*** (0.00)	0.02*** (0.00)
3rd		0.03*** (0.00)	0.01*** (0.00)	0.01* (0.00)		0.02*** (0.00)	0.01* (0.00)	0.01 (0.00)		0.04*** (0.01)	0.02*** (0.01)	0.02*** (0.00)
4th		0.05*** (0.00)	0.02*** (0.00)	0.02*** (0.00)		0.06*** (0.00)	0.02*** (0.00)	0.02*** (0.00)		0.07*** (0.01)	0.03*** (0.01)	0.03*** (0.00)
5th		0.11*** (0.01)	0.05*** (0.01)	0.05*** (0.01)		0.13*** (0.01)	0.05*** (0.00)	0.05*** (0.00)		0.10*** (0.01)	0.03*** (0.01)	0.03*** (0.01)
Immigrant		0.03*** (0.01)	0.03*** (0.00)	0.02*** (0.00)		0.03*** (0.01)	0.02*** (0.01)	0.02*** (0.00)		0.02** (0.01)	0.02*** (0.01)	0.03*** (0.00)
Parents' maximal years of schooling												
12 years		0.04*** (0.00)	0.01*** (0.00)	0.01** (0.00)		0.05*** (0.00)	0.02*** (0.00)	0.01** (0.00)		0.08*** (0.01)	0.04*** (0.01)	0.03*** (0.01)
13-15 years		0.10*** (0.01)	0.04*** (0.00)	0.03*** (0.00)		0.12*** (0.01)	0.04*** (0.01)	0.03*** (0.00)		0.14*** (0.01)	0.06*** (0.01)	0.05*** (0.01)
16 years or more		0.16*** (0.01)	0.06*** (0.01)	0.06*** (0.00)		0.21*** (0.01)	0.09*** (0.01)	0.08*** (0.01)		0.18*** (0.01)	0.08*** (0.01)	0.07*** (0.01)
GEMS												
Mathematics			0.07*** (0.00)	0.07*** (0.00)			0.09*** (0.00)	0.10*** (0.00)			0.05*** (0.00)	0.05*** (0.00)
Science			0.03*** (0.00)	0.02*** (0.00)			0.03*** (0.00)	0.03*** (0.00)			0.04*** (0.00)	0.04*** (0.00)
Reading			0.03*** (0.00)	0.02*** (0.00)			0.03*** (0.00)	0.03*** (0.00)			0.05*** (0.00)	0.04*** (0.00)
English			0.02*** (0.00)	0.02*** (0.00)			0.02*** (0.00)	0.02*** (0.00)			0.01*** (0.00)	0.01*** (0.00)
Mathematics X Reading			0.01*** (0.00)	0.01*** (0.00)			0.02*** (0.00)	0.02*** (0.00)			0.01** (0.00)	0.01* (0.00)
GEMS ²												
Mathematics			0.05*** (0.00)	0.05*** (0.00)			0.07*** (0.00)	0.07*** (0.00)			0.00 (0.00)	0.00 (0.00)
Science			0.02*** (0.00)	0.02*** (0.00)			0.02*** (0.00)	0.02*** (0.00)			0.02*** (0.00)	0.02*** (0.00)
Reading			0.00* (0.00)	0.00 (0.00)			0.01*** (0.00)	0.01*** (0.00)			-0.00 (0.00)	0.00 (0.00)
English			0.01*** (0.00)	0.01*** (0.00)			0.00** (0.00)	0.01*** (0.00)			0.00* (0.00)	0.00** (0.00)
School fixed-effects												
Constant	0.17*** (0.01)	0.04*** (0.01)	0.11*** (0.01)	0.12*** (0.01)	0.16*** (0.01)	0.00 (0.01)	0.09*** (0.01)	0.12*** (0.01)	0.13*** (0.01)	-0.04*** (0.01)	0.04*** (0.01)	0.10*** (0.01)
R ²	0.023	0.081	0.235	0.207	0.005	0.084	0.306	0.277	0.046	0.081	0.164	0.102

Notes: $N_{total} = 68,050$. Dependent variables vary by column: taking physics or computer science; advanced mathematics; and biology or chemistry. Coefficients are obtained from a LPM with school-level clustered standard errors and a dummy for cohort. All GEMS scores are normalized to have a mean of 0 and standard deviation of 1. Standard errors in parentheses. * $p < 0.05$ ** $p < 0.01$ *** $p < 0.001$